

## 5-5 Use Inequalities in a Triangle

Definition of Inequality--  $a > b$  iff there is a positive number  $c$ , such that  $a = b + c$

ex:

$$7 = 3 + 4$$

$$7 > 3 \quad \text{def of inequ.}$$

$$7 > 4$$

# Properties

Transitive

Addition/Subtraction

Multiplication/Division

Subst

Ex:



$$LN = LM + MN \quad \text{SAP}$$

$$LN > LM$$

$$LN > MN \quad \text{def of ineq.}$$

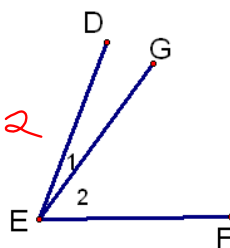
Ex:

$$m\angle DEF = m\angle 1 + m\angle 2$$

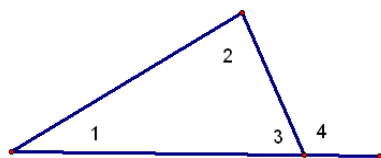
$$m\angle DEF > m\angle 1$$

$$m\angle DEF > m\angle 2$$

(def. of ineq.)



Ex:



$$m\angle 4 = m\angle 1 + m\angle 2$$

$$m\angle 4 > m\angle 1$$

$$m\angle 4 > m\angle 2$$

Exterior Angle Inequality Theorem—The exterior angle of a triangle is greater than either of its corresponding remote interior angles

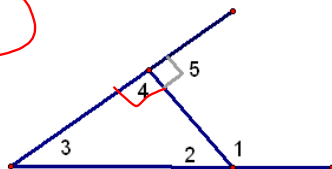


$$m\angle 4 > m\angle 1$$

$$m\angle 4 > m\angle 2$$

Which angle is the largest?

(Figure is not drawn to scale.)



$$m\angle 1 > m\angle 3$$

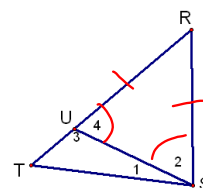
$$m\angle 1 > m\angle 4$$

$$m\angle 1 > m\angle 5$$

$$m\angle 5 > m\angle 3$$

$$m\angle 5 > m\angle 2$$

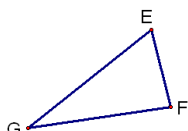
Given:  $\triangle RST$   
 $RU = RS$   
 $RT > RS$

Prove:  $m\angle RST > m\angle T$ 

- |   |                                       |
|---|---------------------------------------|
| ① | Given                                 |
| ② | $\angle 4 \cong \angle 2$             |
| ③ | BAT                                   |
| ④ | $m\angle 4 = m\angle 2$               |
| ⑤ | def of $\cong$                        |
| ⑥ | AAP                                   |
| ⑦ | $m\angle RST = m\angle 1 + m\angle 4$ |
| ⑧ | $m\angle RST > m\angle 2$             |
| ⑨ | def of $>$                            |
| ⑩ | $m\angle RST > m\angle 4$             |
| ⑪ | Subst                                 |
| ⑫ | $m\angle 4 > m\angle T$               |
| ⑬ | Ext. Ang. Thm                         |
| ⑭ | $m\angle RST > m\angle T$             |
| ⑮ | Transitive                            |

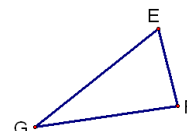
**Theorem 5.10**—If one side of a triangle is longer than another side, then the angle opposite the longer side is larger than the angle opposite the shorter side.

G:  $GE > EF$   
 Concl:  $m\angle F > m\angle G$



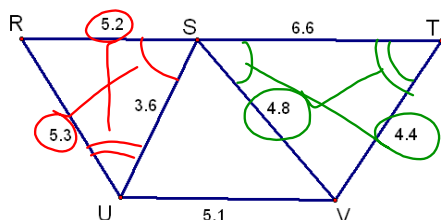
**Theorem 5.11**—If one angle of a triangle is larger than another angle, then the side opposite the larger angle is longer than the side opposite the smaller angle.

Given:  $m\angle F > m\angle G$   
 Concl:  $GE > EF$



1. Which is greater,  $m\angle RSU$  or  $m\angle SUR$ ?

2. Which is greater,  $m\angle TSV$  or  $m\angle STV$ ?



Determine which angle has the greatest measure.

17.  $\angle 1, \angle 2, \angle 4$

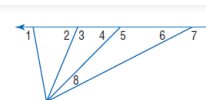
18.  $\angle 2, \angle 4, \angle 6$

19.  $\angle 3, \angle 5, \angle 7$

20.  $\angle 1, \angle 2, \angle 6$

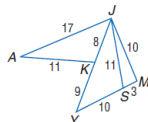
21.  $\angle 5, \angle 7, \angle 8$

22.  $\angle 2, \angle 6, \angle 8$



Determine the relationship between the measures of the given angles.

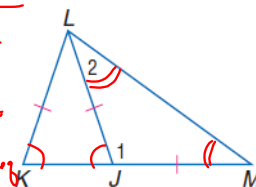
29.  $\angle KAJ$ ,  $\angle AJK$       30.  $\angle MJY$ ,  $\angle JYM$   
 31.  $\angle SMJ$ ,  $\angle MJS$       32.  $\angle AKJ$ ,  $\angle JAK$   
 33.  $\angle MYJ$ ,  $\angle JMY$       34.  $\angle JSY$ ,  $\angle JYS$



35. Given:  $\overline{JM} \cong \overline{JL}$   
 $\overline{JL} \cong \overline{KL}$

Prove:  $m\angle 1 > m\angle 2$

S.	R
①	① Given
② $\angle K \cong \angle LJK$	② BAT
③ $m\angle K = m\angle LJK$	③ def of $\cong$
④ $m\angle 1 > m\angle K$	④ Ext $\angle$ Ineq thm
⑤ $m\angle 1 > m\angle LJK$	⑤ subst
⑥ $m\angle LJK > m\angle 2$	⑥ Ext $\angle$ Ineq thm
⑦ $m\angle 1 > m\angle 2$	⑦ Transitive

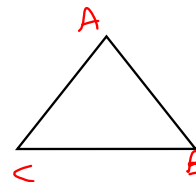


Pasta Challenge



Thm. 5.12--The triangle inequality theorem--the sum of the lengths of any 2 sides of a triangle is greater than the length of the 3rd side.

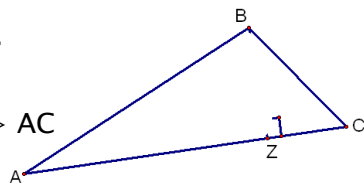
$$\begin{aligned} AB + BC &> AC \\ AB + AC &> BC \\ AC + BC &> AB \end{aligned}$$



Let's Prove it.

Given:  $\triangle ABC$

Prove:  $AB + BC > AC$



Do the lengths represent a triangle?

$(4, 5, 7)$  yes  $4+5 > 7$

$13, 12, 20$  yes  
 $25$

$7, 14, 21$  no  
 $21 = 21$

$7, 7, 7$  yes

$8, 8, 19$  no

Two sides of a triangle are 6 and 11.  
What is the range of the 3rd side?

$$5 < x < 17$$

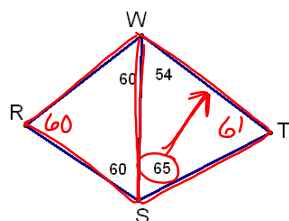
$$\begin{array}{r} 11 \\ -6 \\ \hline 5 \end{array} \qquad \begin{array}{r} 6 \\ +11 \\ \hline 17 \end{array}$$

Two sides of a triangle are 12 and 18.  
What is the range of the 3rd side?

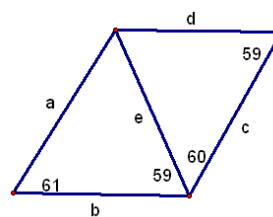
$$6 < x < 30$$

What is the longest segment?

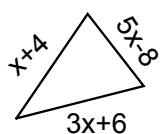
WT



What is the longest segment?



Describe the possible values for x.



$$\begin{aligned} 5x - 8 &> 0 \\ x &> \frac{8}{5} \\ 3x + 6 &> 0 \\ x &> -2 \\ x + 4 &> 0 \\ x &> -4 \end{aligned}$$

$$x + 4 + 3x + 6 > 5x - 8$$

$$18 > x$$

$$x + 4 + 5x - 8 > 3x + 6$$

$$x > \frac{10}{3}$$

$$3x + 6 + 5x - 8 > x + 4$$

$$x > \frac{6}{7}$$

$$\frac{10}{3} < x < 18$$

HW p331-332

#s 6, 10-13, 16-19, 21-23, 30, 31, 33, 34